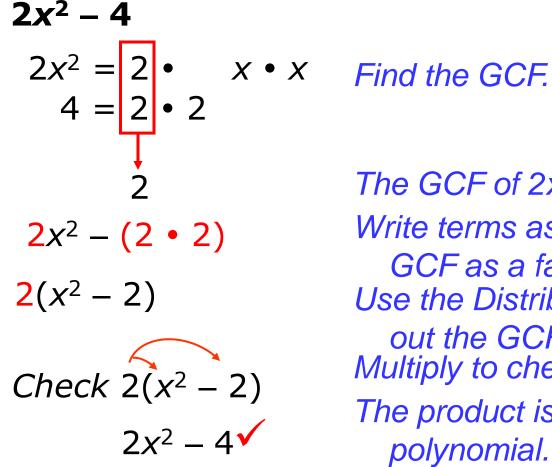
Recall that the Distributive Property states that ab + ac = a(b + c). The Distributive Property allows you to "factor" out the GCF of the terms in a polynomial to write a factored form of the polynomial.

A polynomial is in its factored form when it is written as a product of monomials and polynomials that cannot be factored further. The polynomial 2(3x - 4x) is not fully factored because the terms in the parentheses have a common factor of *x*.

Example 1A: Factoring by Using the GCF

http://my.hrw.com/math11/math06_07/nsmedia/lesson_videos/alg1/play er.html?contentSrc=6366/6366.xml

Factor each polynomial. Check your answer.



The GCF of 2x² and 4 is 2.
Write terms as products using the GCF as a factor.
Use the Distributive Property to factor out the GCF.
Multiply to check your answer.
The product is the original polynomial.

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Example 1B: Factoring by Using the GCF Factor each polynomial. Check your answer. $8x^3 - 4x^2 - 16x$

The GCF of 8x³, 4x², and 16x is 4x.

 Write terms as products using the GCF as a factor.
 Use the Distributive Property to factor out the GCF.

Multiply to check your answer. The product is the original polynomials.

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Example 1C: Factoring by Using the GCF Factor each polynomial. Check your answer.

- $-14x 12x^2$
- $-1(14x + 12x^2)$





Example 1C: Factoring by Using the GCF Factor each polynomial. Check your answer.

 $-14x - 12x^2$

Check

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Caution!

When you factor out -1 as the first step, be sure to include it in all the other steps as well.

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Check It Out! Example 1c

Factor each polynomial. Check your answer.

 $-18y^3 - 7y^2$

Both coefficients are negative. Factor out –1. Find the GCF. The GCF of $18y^3$ and $7y^2$ is y^2 . Write each term as a product using the GCF. Use the Distributive Property to factor out the GCF.

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Check It Out! Example 1d

Factor each polynomial. Check your answer.

 $8x^4 + 4x^3 - 2x^2$

Find the GCF.

The GCF of 8x⁴, 4x³ and -2x² is 2x².
Write terms as products using the GCF as a factor.
Use the Distributive Property to factor out the GCF.
Multiply to check your answer.

The product is the original polynomial.

To write expressions for the length and width of a rectangle with area expressed by a polynomial, you need to write the polynomial as a product. You can write a polynomial as a product by factoring it.

Example 2: *Application*

http://my.hrw.com/math11/math06_07/nsmedia/lesson_videos/alg1/play er.html?contentSrc=7548/7548.xml

The area of a court for the game squash is $9x^2 + 6x m^2$. Factor this polynomial to find possible expressions for the dimensions of the squash court.

 $A = 9x^2 + 6x$ The GCF of $9x^2$ and 6x is 3x.= 3x(3x) + 2(3x)Write each term as a product
using the GCF as a factor.= 3x(3x + 2)Use the Distributive Property to
factor out the GCF.

Possible expressions for the dimensions of the squash court are 3x m and (3x + 2) m.



Check It Out! Example 2

What if...? The area of the solar panel on another calculator is $(2x^2 + 4x)$ cm². Factor this polynomial to find possible expressions for the dimensions of the solar panel.

$$A = 2x^2 + 4x$$

The GCF of $2x^2$ and 4x is 2x.

Write each term as a product using the GCF as a factor.Use the Distributive Property to factor out the GCF. Sometimes the GCF of terms is a binomial. This GCF is called a common binomial factor. You factor out a common binomial factor the same way you factor out a monomial factor.

Example 3: Factoring Out a Common Binomial Factor

http://my.hrw.com/math11/math06_07/nsmedia/lesson_videos/alg1/player.h tml?contentSrc=7549/7549.xml

Factor each expression.

A. 5(x + 2) + 3x(x + 2)

5(x + 2) + 3x(x + 2)

(x + 2)(5 + 3x)

The terms have a common binomial factor of (x + 2). Factor out (x + 2).

B. $-2b(b^2 + 1) + (b^2 + 1)$

The terms have a common binomial factor of $(b^2 + 1)$. $(b^2 + 1) = 1(b^2 + 1)$

Factor out $(b^2 + 1)$.



Example 3: Factoring Out a Common Binomial Factor

Factor each expression. C. $4z(z^2 - 7) + 9(2z^3 + 1)$

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You may be able to factor a polynomial by grouping. When a polynomial has four terms, you can make two groups and factor out the GCF from each group.

Example 4A: Factoring by Grouping

http://my.hrw.com/math11/math06_07/nsmedia/lesson_videos/alg1/playe r.html?contentSrc=7550/7550.xml

Factor each polynomial by grouping. Check your answer.

- $6h^4 4h^3 + 12h 8$
 - $(6h^4 4h^3) + (12h 8)$ Group terms that have a common number or variable as a factor.
 - $2h^{3}(3h-2) + 4(3h-2)$ Factor out the GCF of each group.

$$2h^{3}(3h-2) + 4(3h-2)$$

 $(3h-2)(2h^3+4)$ Factor out (3h-2).



Example 4A Continued

Factor each polynomial by grouping. Check your answer.

Check
$$(3h - 2)(2h^3 + 4)$$

Multiply to check your solution.

 $3h(2h^3) + 3h(4) - 2(2h^3) - 2(4)$

 $6h^4 + 12h - 4h^3 - 8$

 $6h^4 - 4h^3 + 12h - 8^{\checkmark}$

The product is the original polynomial.



Example 4B: Factoring by Grouping

Factor each polynomial by grouping. Check your answer.

 $5y^4 - 15y^3 + y^2 - 3y$

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Example 4B Continued

Factor each polynomial by grouping. Check your answer.

 $5y^4 - 15y^3 + y^2 - 3y$

Check

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Helpful Hint

If two quantities are opposites, their sum is 0. (5 - x) + (x - 5) 5 - x + x - 5 - x + x + 5 - 5 0 + 0 0

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Recognizing opposite binomials can help you factor polynomials. The binomials (5 - x) and (x - 5) are opposites. Notice (5 - x) can be written as -1(x - 5).

$$-1(x-5) = (-1)(x) + (-1)(-5)$$

$$= -x + 5$$

$$= 5 - x$$

$$50, (5-x) = -1(x-5)$$
Distributive Property of Addition.

Example 5: Factoring with Opposites http://my.hrw.com/math11/math06_07/nsmedia/lesson_videos/alg1/player .html?contentSrc=7551/7551.xml

Factor $2x^3 - 12x^2 + 18 - 3x$

$$2x^3 - 12x^2 + 18 - 3x$$

$$(2x^3 - 12x^2) + (18 - 3x)$$

Group terms.

$$2x^{2}(x-6) + 3(6-x)$$
$$2x^{2}(x-6) + 3(-1)(x-6)$$

$$2x^2(x-6) - 3(x-6)$$

$$(x-6)(2x^2-3)$$

Factor out the GCF of each group. Write (6 - x) as -1(x - 6).

Simplify. (x - 6) is a common factor. Factor out (x - 6).



Check It Out! Example 5b

Factor each polynomial. Check your answer.

8y - 8 - x + xy

Group terms.

Factor out the GCF of each group.
(y – 1) is a common factor.
Factor out (y – 1).

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